

A(nother) Sample Model for Predicate Logic (PredL)

The domain D simply lists all of the “inhabitants” of our model:

$$D = \{ \text{Alice, Bill, Clive, Damien, Latoya, Marcia, Olivia, Paul} \}$$

The assignment function Val establishes a relationship between the “words” of PredL and the “inhabitants” of our model:

1. Individual constants denote specific inhabitants of our model.

$$Val(a) = \text{Alice}$$

$$Val(l) = \text{Latoya}$$

$$Val(b) = \text{Bill}$$

$$Val(m) = \text{Marcia}$$

$$Val(c) = \text{Clive}$$

$$Val(o) = \text{Olivia}$$

$$Val(d) = \text{Damien}$$

$$Val(p) = \text{Paul}$$

2. One-place predicates express properties, and so denote sets of individuals.

$$Val(\text{RICH}) = \{ \text{Paul, Alice, Marcia, Olivia, Bill} \}$$

$$Val(\text{GENEROUS}) = \{ \text{Olivia, Clive} \} \quad Val(\text{SURGEON}) = \{ \text{Latoya, Alice} \}$$

$$Val(\text{LAUGH}) = \{ \text{Paul, Alice, Marcia, Damien} \}$$

3. Two-place predicates express relations that can hold between two individuals, and so denote sets of ordered pairs of individuals.

$$Val(\text{HUG}) = \{ \langle \text{Clive, Marcia} \rangle, \langle \text{Marcia, Clive} \rangle, \langle \text{Paul, Marcia} \rangle \}$$

$$Val(\text{MARRY}) = \{ \langle \text{Bill, Latoya} \rangle, \langle \text{Damien, Marcia} \rangle, \langle \text{Clive, Olivia} \rangle \}$$

4. Three-place predicates express relations that can hold between three individuals, and so denote sets of ordered triplets of individuals.

$$Val(\text{INTRODUCE}) = \{ \langle \text{Marcia, Bill, Latoya} \rangle, \langle \text{Marcia, Olivia, Clive} \rangle \}$$

Using the provide key, translate the following English sentences into PredL.
Then, determine whether the PredL formulas are true in the above model.

a : Alice l : Latoya SURGEON(x) : x is a surgeon
b : Bill m : Marcia RICH(x) : x is rich
c : Clive o : Olivia GENEROUS(x) : x is generous
d : Damien p : Paul LAUGH(x) : x laugh

HUG(x, y) : x hug y INTRODUCE(x, y, z) : x introduce y to z
MARRY (x, y) : x marry y

- (1) Olivia is a surgeon. (2) Bill was introduced to Latoya by Marcia.
- (3) Paul is not both rich and generous.
- (4) Neither Alice nor Bill laughed.
- (5) Bill and Damien respectively married Latoya and Olivia.
- (6) Clive and Marcia hugged.